Big bang nucleosynthesis: Present status

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Big bang nucleosynthesis (BBN) describes the production of the lightest nuclides via a dynamic interplay among the four fundamental forces during the first seconds of cosmic time. A brief overview of the essentials of this physics is given, and new calculations presented of light-element abundances through ⁶Li and ⁷Li, with updated nuclear reactions and uncertainties including those in the neutron lifetime. Fits are provided for these results as a function of baryon density and of the number of neutrino flavors N_u. Recent developments are reviewed in BBN, particularly new, precision Planck cosmic microwave background (CMB) measurements that now probe the baryon density, helium content, and the effective number of degrees of freedom $N_{\rm eff}$. These measurements allow for a tight test of BBN and cosmology using CMB data alone. Our likelihood analysis convolves the 2015 Planck data chains with our BBN output and observational data. Adding astronomical measurements of light elements strengthens the power of BBN. A new determination of the primordial helium abundance is included in our likelihood analysis. New D/H observations are now more precise than the corresponding theoretical predictions and are consistent with the standard model and the Planck baryon density. Moreover, D/H now provides a tight measurement of N_{ν} when combined with the CMB baryon density and provides a 2σ upper limit $N_{\nu} < 3.2$. The new precision of the CMB and D/H observations together leaves D/H predictions as the largest source of uncertainties. Future improvement in BBN calculations will therefore rely on improved nuclear cross-section data. In contrast with D/H and ⁴He, ⁷Li predictions continue to disagree with observations, perhaps pointing to new physics. This paper concludes with a look at future directions including key nuclear reactions, astronomical observations, and theoretical issues.

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I. INTRODUCTION

Big bang nucleosynthesis (BBN) is one of the few probes of the very early Universe with direct experimental or observational consequences (Walker *et al.*, 1991; Olive, Steigman, and Walker, 2000; Fields and Olive, 2006; Steigman, 2007; Iocco *et al.*, 2009; Fields, Molaro, and Sarkar, 2014). In the context of the standard models of cosmology and of nuclear and particle physics, BBN is an effectively parameter-free

 $\pm 1\sigma$ spread in the predicted abundances. These results assume $N_{\nu}=3$ and the current measurement of the neutron lifetime $\tau_n=880.3\pm1.1$ s.

Using a Monte Carlo approach also allows us to extract sensitivities of the light-element predictions to reaction rates and other parameters. The sensitivities are defined as the logarithmic derivatives of the light-element abundances with respect to each variation about our fiducial model parameters (Fiorentini *et al.*, 1998), yielding a simple relation for extrapolating about the fiducial model:

$$X_i = X_{i,0} \prod_n \left(\frac{p_n}{p_{n,0}}\right)^{\alpha_n},\tag{12}$$

where X_i represents either the helium mass fraction or the abundances of the other light elements by number. The p_n represent input quantities to the BBN calculations (η, N_{ν}, τ_n) and the gravitational constant⁵ G_N as well as key nuclear rates which affect the abundance X_i . $p_{n,0}$ refers to our standard input value. The information contained in Eqs. (13)–(17) is summarized in Table III:

$$Y_{p} = 0.24703 \left(\frac{10^{10} \eta}{6.10}\right)^{0.039} \left(\frac{N_{\nu}}{3.0}\right)^{0.163} \left(\frac{G_{N}}{G_{N,0}}\right)^{0.35} \left(\frac{\tau_{n}}{880.3s}\right)^{0.73} [p(n,\gamma)d]^{0.005} [d(d,n)^{3} \text{He}]^{0.006} [d(d,p)t]^{0.005},$$
(13)

$$\frac{\mathrm{D}}{\mathrm{H}} = 2.579 \times 10^{-5} \left(\frac{10^{10} \eta}{6.10}\right)^{-1.60} \left(\frac{N_{\nu}}{3.0}\right)^{0.395} \left(\frac{G_N}{G_{N,0}}\right)^{0.95} \left(\frac{\tau_n}{880.3s}\right)^{0.41} [p(n,\gamma)d]^{-0.19} [d(d,n)^3 \mathrm{He}]^{-0.53} [d(d,p)t]^{-0.47} \\
\times [d(p,\gamma)^3 \mathrm{He}]^{-0.31} [^3 \mathrm{He}(n,p)t]^{0.023} [^3 \mathrm{He}(d,p)^4 \mathrm{He}]^{-0.012}, \tag{14}$$

$$\frac{^{3}\text{He}}{\text{H}} = 9.996 \times 10^{-6} \left(\frac{10^{10} \eta}{6.10}\right)^{-0.59} \left(\frac{N_{\nu}}{3.0}\right)^{0.14} \left(\frac{G_{N}}{G_{N.0}}\right)^{0.34} \left(\frac{\tau_{n}}{880.3s}\right)^{0.15} [p(n,\gamma)d]^{0.088} [d(d,n)^{3}\text{He}]^{0.21} [d(d,p)t]^{-0.27} \times [d(p,\gamma)^{3}\text{He}]^{0.38} [^{3}\text{He}(n,p)t]^{-0.17} [^{3}\text{He}(d,p)^{4}\text{He}]^{-0.76} [t(d,n)^{4}\text{He}]^{-0.009},$$
(15)

$$\frac{{}^{7}\text{Li}}{\text{H}} = 4.648 \times 10^{-10} \left(\frac{10^{10} \eta}{6.10}\right)^{2.11} \left(\frac{N_{\nu}}{3.0}\right)^{-0.284} \left(\frac{G_{N}}{G_{N,0}}\right)^{-0.73} \left(\frac{\tau_{n}}{880.3s}\right)^{0.43} [p(n,\gamma)d]^{1.34} [d(d,n)^{3}\text{He}]^{0.70} [d(d,p)t]^{0.065} \\
\times [d(p,\gamma)^{3}\text{He}]^{0.59} [^{3}\text{He}(n,p)t]^{-0.27} [^{3}\text{He}(d,p)^{4}\text{He}]^{-0.75} [t(d,n)^{4}\text{He}]^{-0.023} \\
\times [^{3}\text{He}(\alpha,\gamma)^{7}\text{Be}]^{0.96} [^{7}\text{Be}(n,p)^{7}\text{Li}]^{-0.71} [^{7}\text{Li}(p,\alpha)^{4}\text{He}]^{-0.056} [t(\alpha,\gamma)^{7}\text{Li}]^{0.030}, \tag{16}$$

$$\frac{^{6}\text{Li}}{\text{H}} = 1.288 \times 10^{-13} \left(\frac{10^{10} \eta}{6.10}\right)^{-1.51} \left(\frac{N_{\nu}}{3.0}\right)^{0.60} \left(\frac{G_{N}}{G_{N,0}}\right)^{1.40} \left(\frac{\tau_{n}}{880.3s}\right)^{1.37} [p(n,\gamma)d]^{-0.19} [d(d,n)^{3}\text{He}]^{-0.52} [d(d,p)t]^{-0.46} \\
\times [d(p,\gamma)^{3}\text{He}]^{-0.31} [^{3}\text{He}(n,p)t]^{0.023} [^{3}\text{He}(d,p)^{4}\text{He}]^{-0.012} [d(\alpha,\gamma)^{6}\text{Li}]^{1.00}.$$
(17)

B. The neutron mean lifetime

As noted in the Introduction, the value of the neutron mean lifetime has had a turbulent history. Unfortunately, the predictions of SBBN remain sensitive to this quantity. This sensitivity is displayed in the scatter plot of our Monte Carlo error propagation with fixed $\eta=6.10\times10^{-10}$ in Fig. 2. The correlation between the neutron mean lifetime and ⁴He abundance prediction is clear. The correlation is not infinitesimally narrow because other reaction rate uncertainties significantly contribute to the total uncertainty in ⁴He.

C. Planck likelihood functions

For this paper, we consider two sets of *Planck* Markov chain data, one for standard BBN (SBBN) and one for

TABLE III. The sensitivities α_n 's defined in Eq. (12) for each of the light-element abundance predictions, varied with respect to key parameters and reaction rates.

Variant	Y_p	D/H	³ He/H	⁷ Li/H	⁶ Li/H
$\eta (6.1 \times 10^{-10})$	0.039	-1.598	0.585	2.113	-1.512
N_{ν} (3.0)	0.163	0.395	0.140	-0.284	0.603
G_N	0.354	0.948	0.335	-0.727	1.400
n decay	0.729	0.409	0.145	0.429	1.372
$p(n,\gamma)d$	0.005	-0.194	0.088	1.339	-0.189
3 He $(n, p)t$	0.000	0.023	-0.170	-0.267	0.023
7 Be $(n, p)^{7}$ Li	0.000	0.000	0.000	-0.705	0.000
$d(p,\gamma)^3$ He	0.000	-0.312	0.375	0.589	-0.311
$d(d, \gamma)^4$ He	0.000	0.000	0.000	0.000	0.000
$^{7}\mathrm{Li}(p,\alpha)^{4}\mathrm{He}$	0.000	0.000	0.000	-0.056	0.000
$d(\alpha, \gamma)^6$ Li	0.000	0.000	0.000	0.000	1.000
$t(\alpha, \gamma)^7$ Li	0.000	0.000	0.000	0.030	0.000
3 He $(\alpha, \gamma)^{7}$ Be	0.000	0.000	0.000	0.963	0.000
$d(d,n)^3$ He	0.006	-0.529	0.213	0.698	-0.522
d(d, p)t	0.005	-0.470	-0.265	0.065	-0.462
$t(d, n)^4$ He	0.000	0.000	-0.009	-0.023	0.000
$^{3}\text{He}(d,p)^{4}\text{He}$	0.000	0.012	-0.762	-0.752	-0.012

 $^{^5}$ In models beyond the standard model, one may also consider variations of the gravitational constant (for fixed nucleon masses). See Yang *et al.* (1979), Accetta, Krauss, and Romanelli (1990), Sarkar (1996), Copi, Davis, and Krauss (2004), and Cyburt *et al.* (2005) for BBN limits on variations of G_N .